

# Drying of cohesive particles in vibrated fluidized beds

## Modeling hydrodynamics under mechanical vibration

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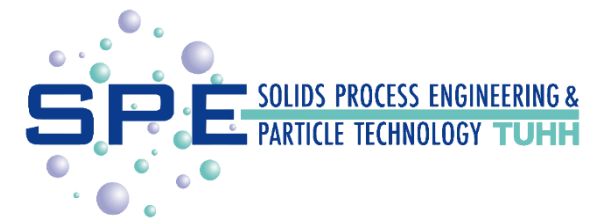
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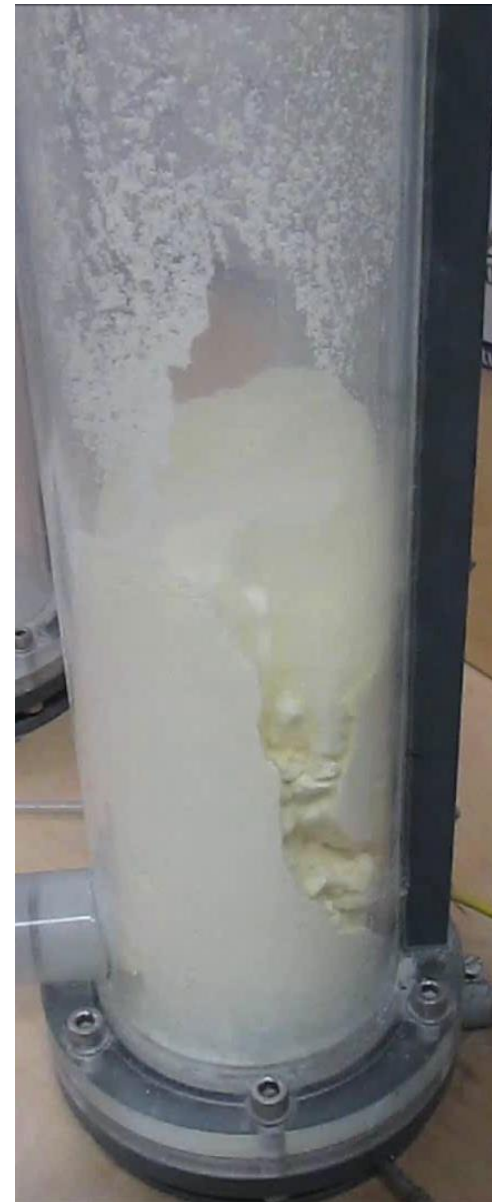
*Tetra Pak Processing Systems, Lund, Sweden*

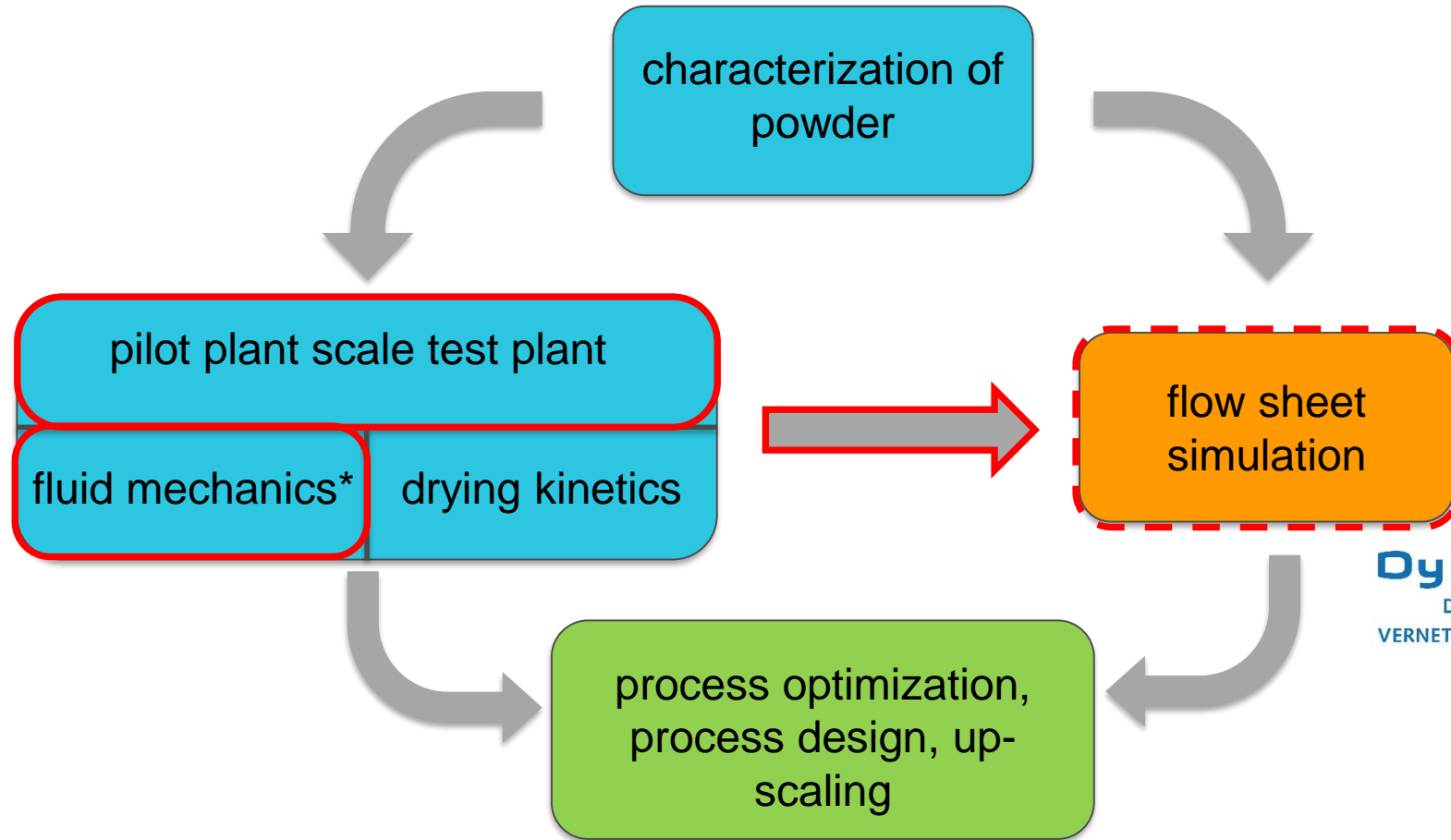


**Cohesive powders gain importance:**  
nano-particles, pharmaceutical and food powders

**Vibration enhances fluidization of cohesive powders:**

- vibrated fluidized bed (VFB) research only in lab-scale
- scarce research on VFB drying of milk powder





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\* Lehmann et al., Fluidization characteristics of cohesive powders in vibrated fluidized bed drying at low vibration frequencies, Powder Technology, accepted

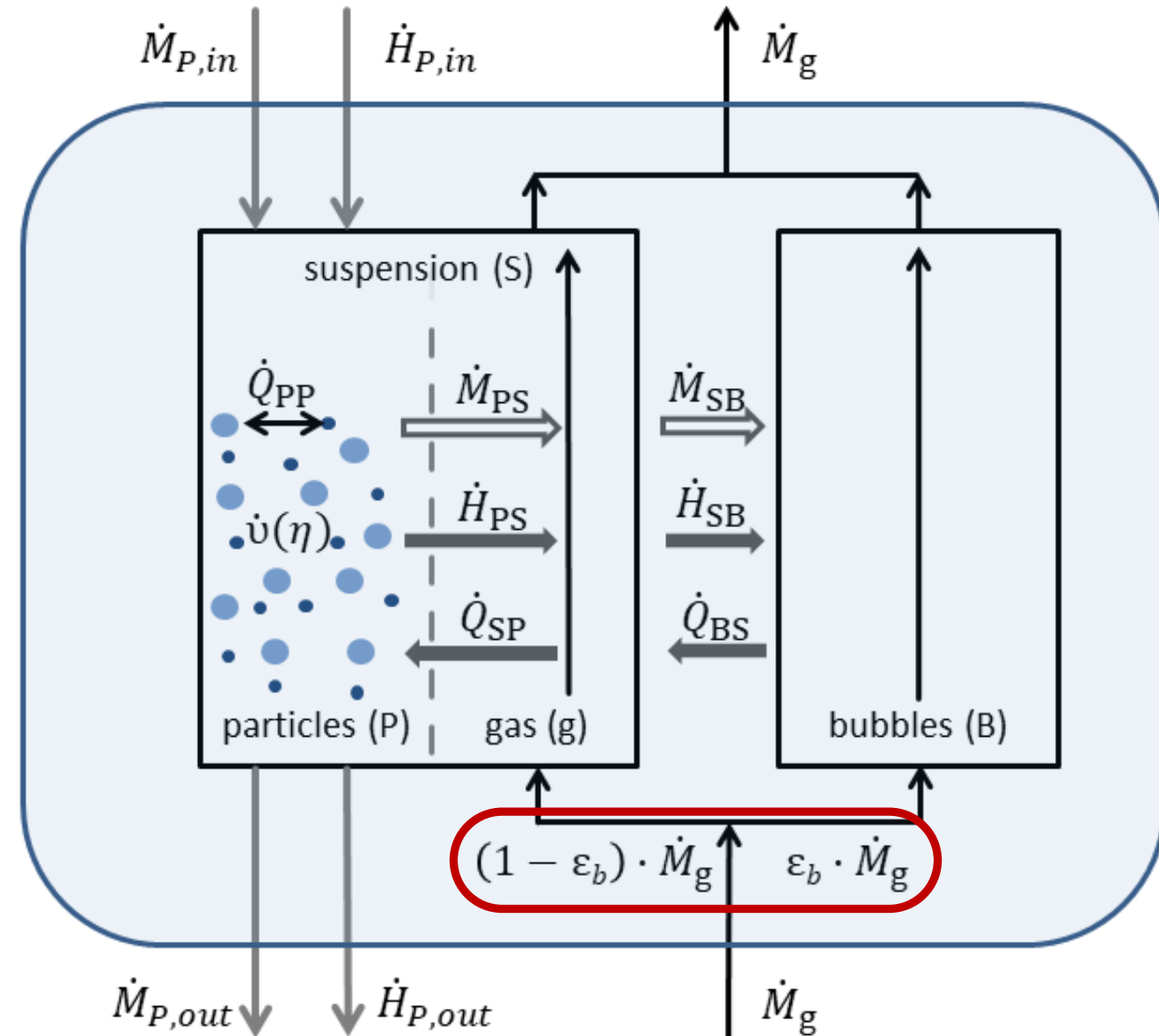


### Basis: Alaathar [1,2]

- steady state model of continuous fluidized bed dryers
- for Geldart B particles
- distributed parameters:  $T$ ,  $d_p$ ,  $x$ ,  $\tau$
- drying kinetics model [3 - 5]
- fluid mechanics model [6]
- key parameter:  
bubble volume fraction  $\varepsilon_b$

### Required adjustments:

- dynamic model
- cohesive powders
- influence of vibration



[1] Alaathar et al., Powder Technology 238, (2013)

[2] Alaathar, PhD Thesis, TUHH, (2017)

[3] Groenewold and Tsotsas, Drying Technology, 15 (1997)

[4] Burgschweiger et al., Can. Journ. of Chem. Engin., 77 (1999)

[5] Burgschweiger and Tsotsas, Chem. Engin. Science, 57 (2002)

[6] Werther and Wein, AIChE Symp., 90 (1994)

### Material:

Whole milk powder	
$\rho_s$ [kg/m <sup>3</sup> ]	866.4±73.5
$d_{32}$ [μm]	101.7±1.3

### Investigated process parameters:

- gas flow rate
- vibration intensity  $\Lambda$

$$\Lambda = \frac{a_{vibration}}{g} = \frac{(2\pi f)^2 \cdot A_{vib}}{g}$$



Whole milk powder:

$x = 4$  wt.-%;  $m = 12.5$  kg;  $u = 0.3$  m/s;  $\Lambda = 0.58$

### Analysis of fluid mechanics via:

- $\Delta p$  measurement
- visual observation (high speed camera)

### Characteristics:

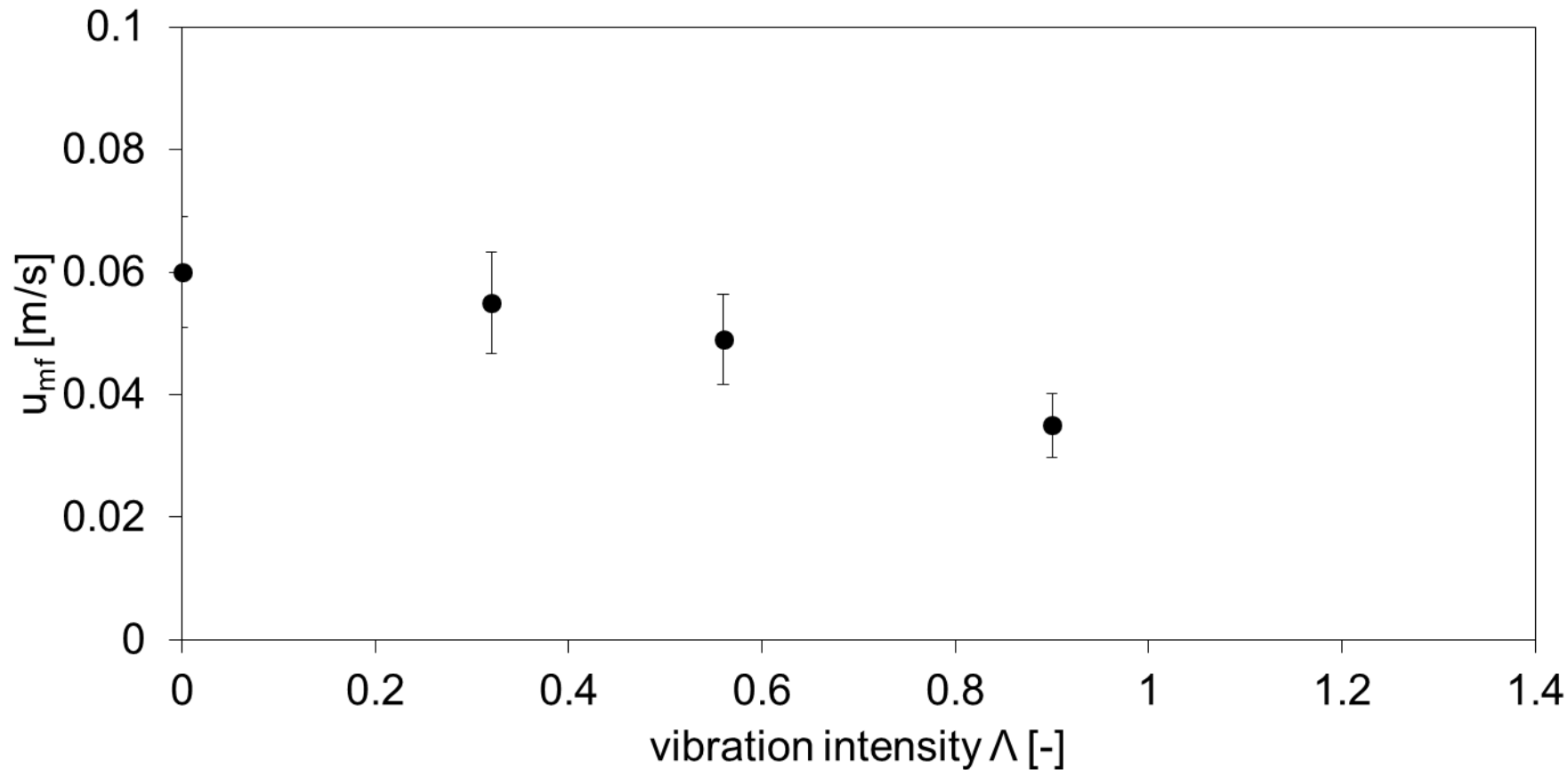
- bed expansion
- gas hold-up / bubble volume fraction
- lower limit of fluidization ( $u_{mf}$ )

frequency	$f$	[Hz]	0	4	6	8	10
amplitude	$A_{vib}$	[mm]	0	5	4	3.5	3
intensity	$\Lambda$	[-]	0	0.32	0.58	0.90	1.21

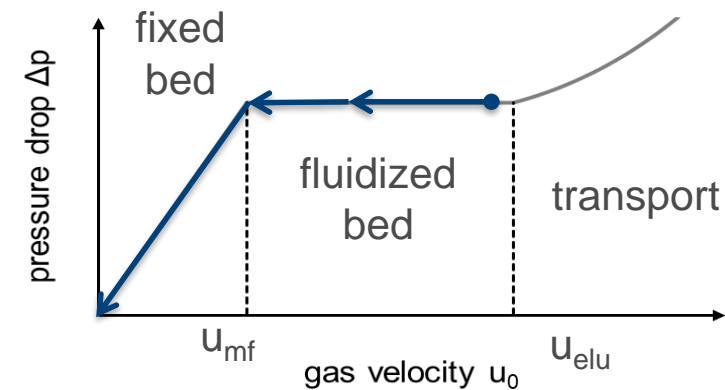
$\rho_s$ : particle density;  $d_{32}$ : Sauter mean diameter;  $X$ : powder moisture content;  $f$ : frequency;  $A_{vib}$ : amplitude,  $g$ : gravitational acceleration;  $\Lambda$ : vibration intensity

Whole milk powder:  
 $x = 4 \text{ wt.}\%$   
 $m = 25 \text{ kg}$

### Minimum fluidization velocity $u_{mf}$ :



### Determination method:

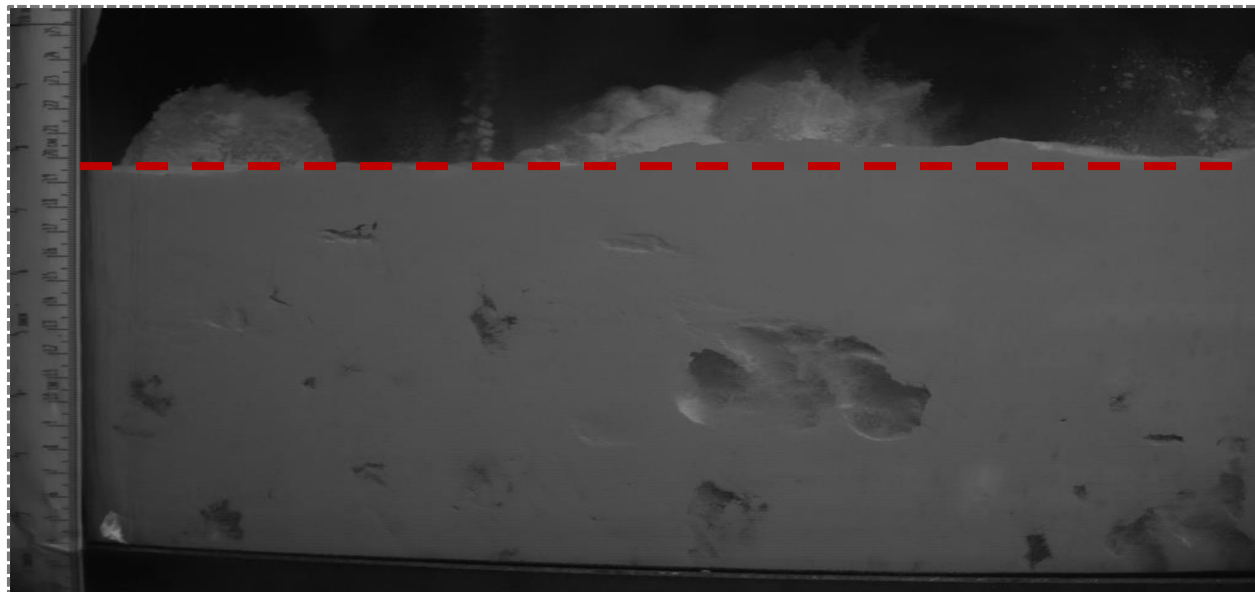


- vibration decreases  $u_{mf}$

Whole milk powder:  $x = 4$  wt.%,  $m = 12.5$  kg;  $\varepsilon_{\text{bulk}} = 0.53$

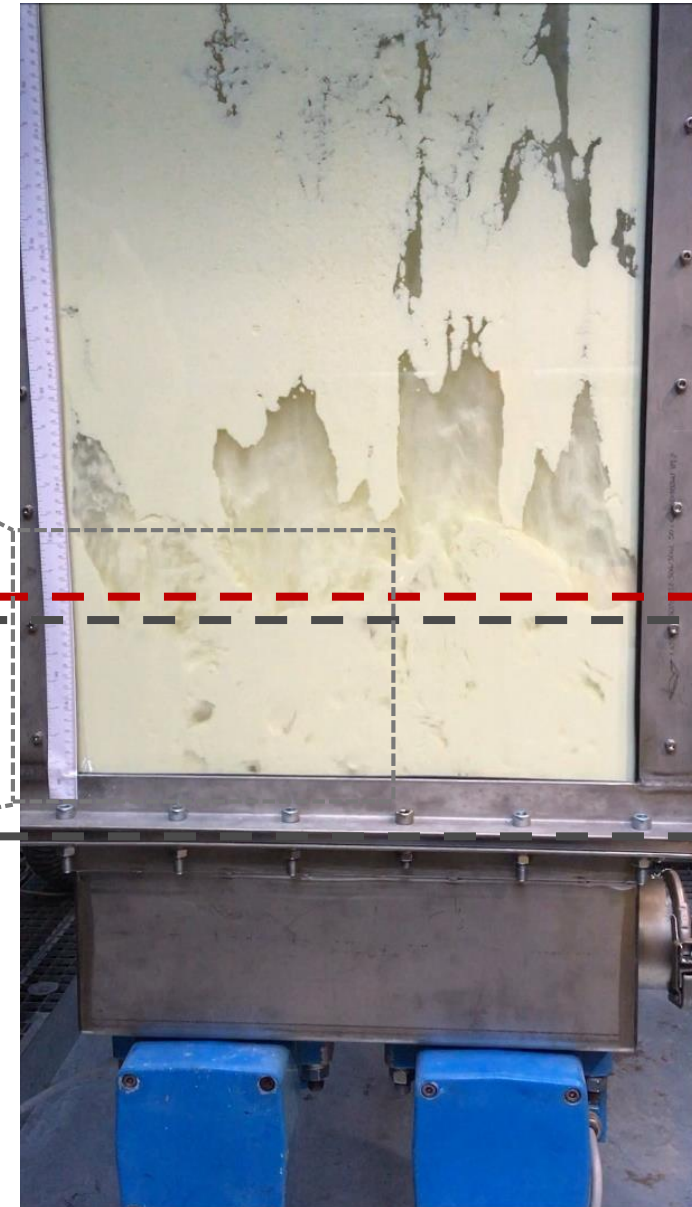
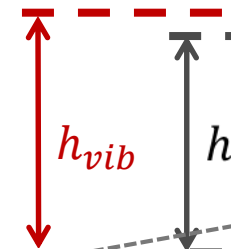
### Bed expansion:

- read bed height  $h$  from high speed camera images



- ca 0      0.05      0.10      0.15      0.20      0.25

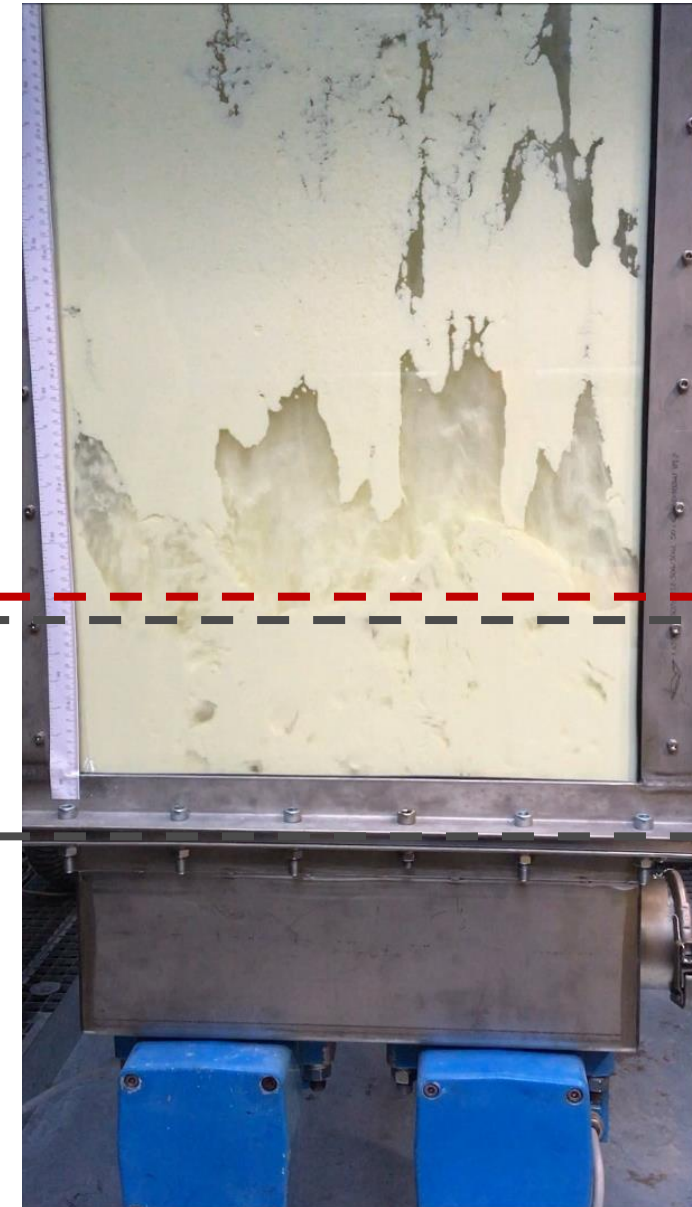
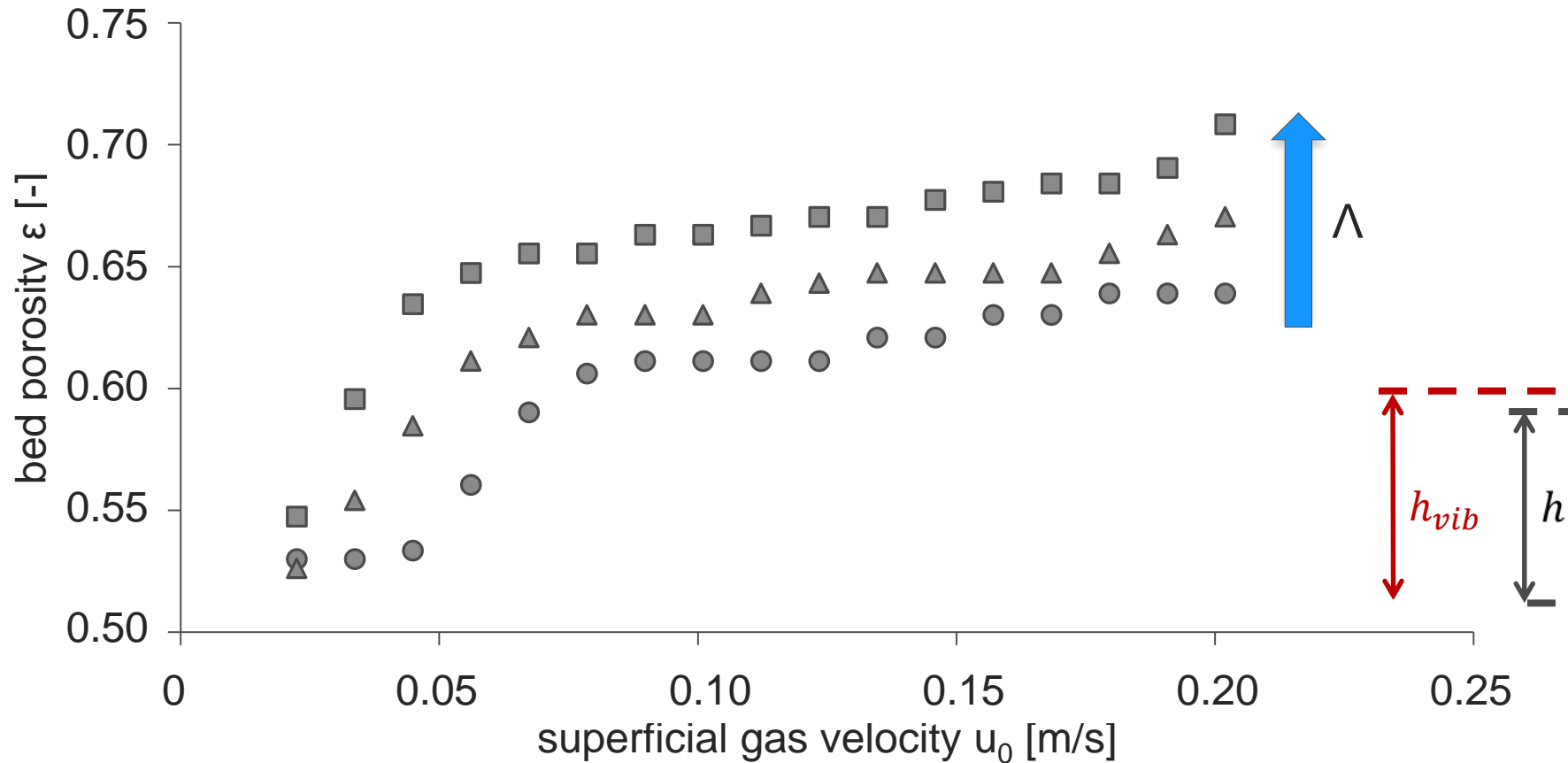
$$\varepsilon = 1 - \frac{m}{A \cdot h \cdot \rho_s}$$



Whole milk powder:  $x = 4$  wt.%,  $m = 12.5$  kg;  $\epsilon_{\text{bulk}} = 0.53$

### Bed expansion:

●  $\Lambda = 0$     ▲  $\Lambda = 0.58$     ■  $\Lambda = 1.21$



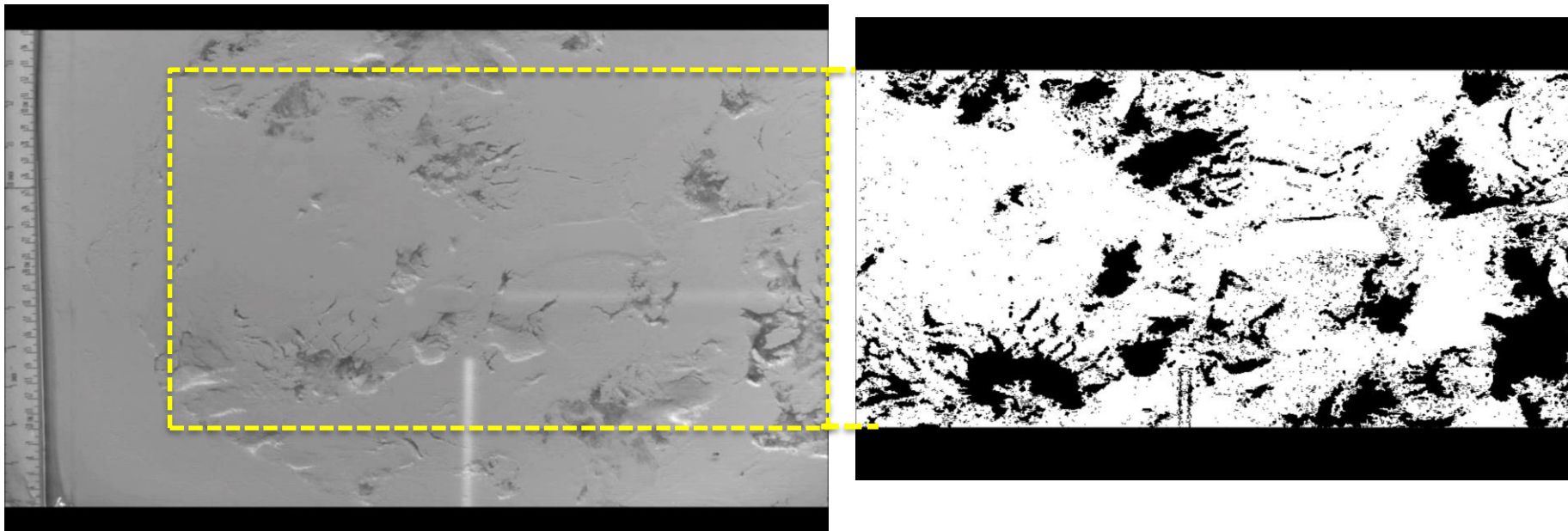
- high bed expansion indicates Geldart A behavior
- vibration increases bed expansion



**Image analysis:**

- high speed image series (100 fps)
- segmentation of grey scale image series (Matlab)
- calculate bubble volume fraction (Matlab)
- non-invasive
- global measurement
- only at the glass wall (2D plane)

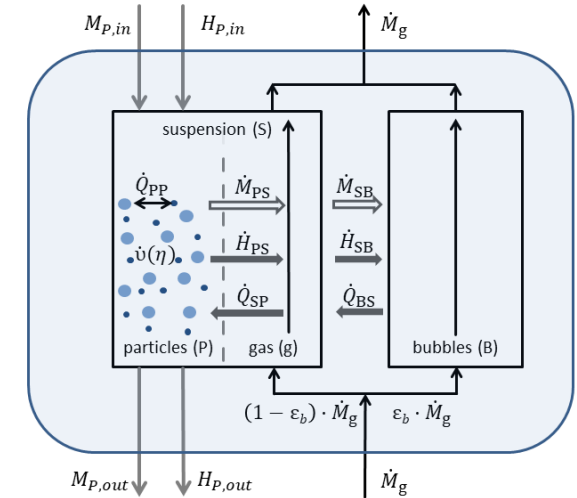
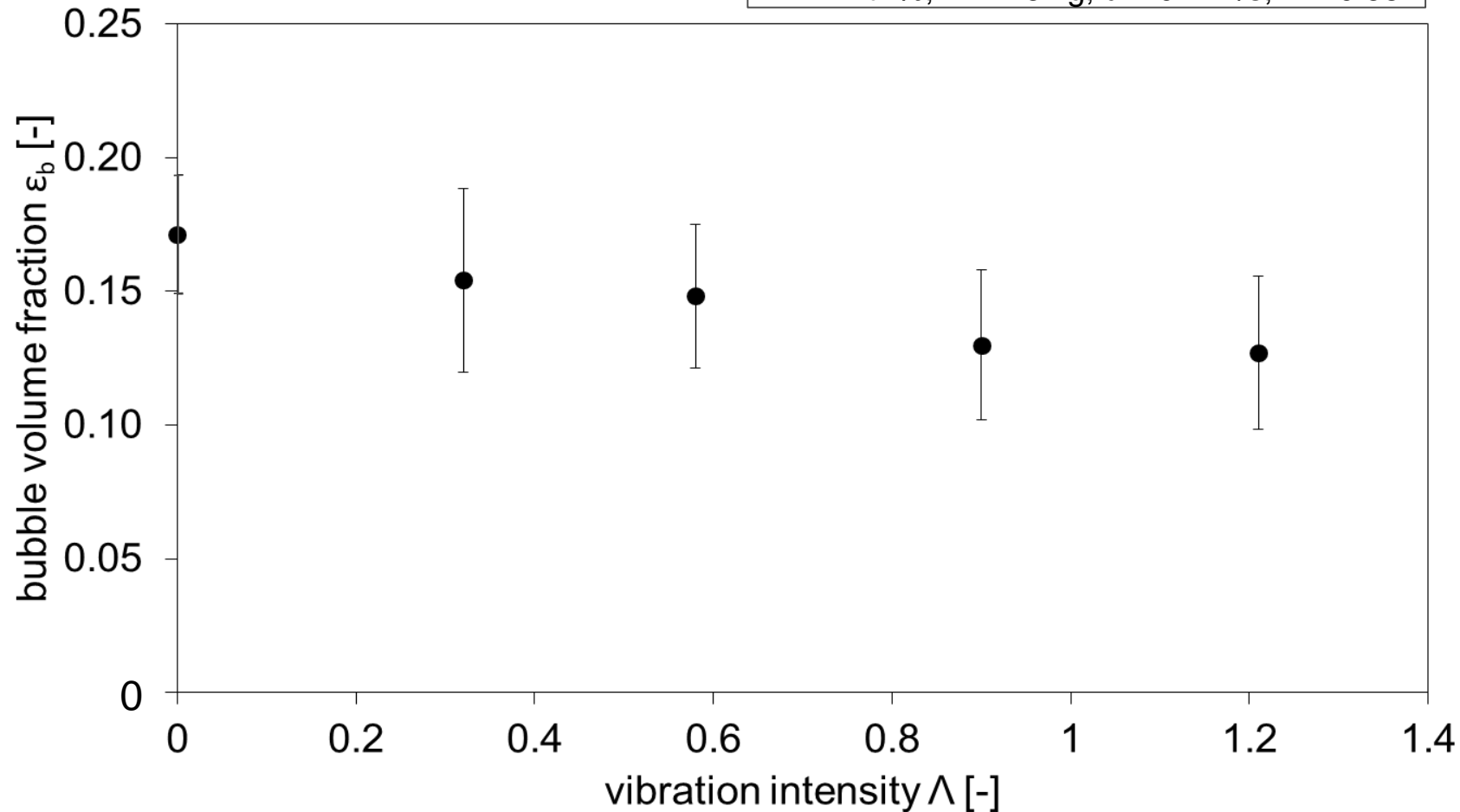
**Valid representation of hydrodynamics inside the bed for  
low excess gas velocities ( $u-u_{mf} < 0.25$ ) [7]**



[7] Lehmann et al., Fluidization characteristics of cohesive powders in vibrated fluidized bed drying at low vibration frequencies, Powder Technology, accepted

### Bubble volume fraction $\varepsilon_b$ :

Whole milk powder:  
 $x = 4 \text{ wt.-%}$ ;  $m = 25 \text{ kg}$ ;  $u = 0.2 \text{ m/s}$ ;  $\Lambda = 0.58$



- slight decrease of bubble volume fraction
- increase of bed expansion
- vibration causes expansion of suspension phase
- explains increased heat and mass transfer rates

### Bubble volume fraction:

- modified correlation from Hillgardt and Werther [8]

$$\varepsilon_b = \frac{\dot{V}_b}{u_b}$$

$$u_b = \dot{V}_b + 0.71 \cdot \vartheta \cdot \sqrt{g \cdot d_v}$$

$$\dot{V}_b = \Psi \cdot (u - u_{mf}) \cdot \frac{1}{(1 + \Lambda)}$$

### Bubble diameter:

- correlation from Zou et al. [9]
- for cohesive particles

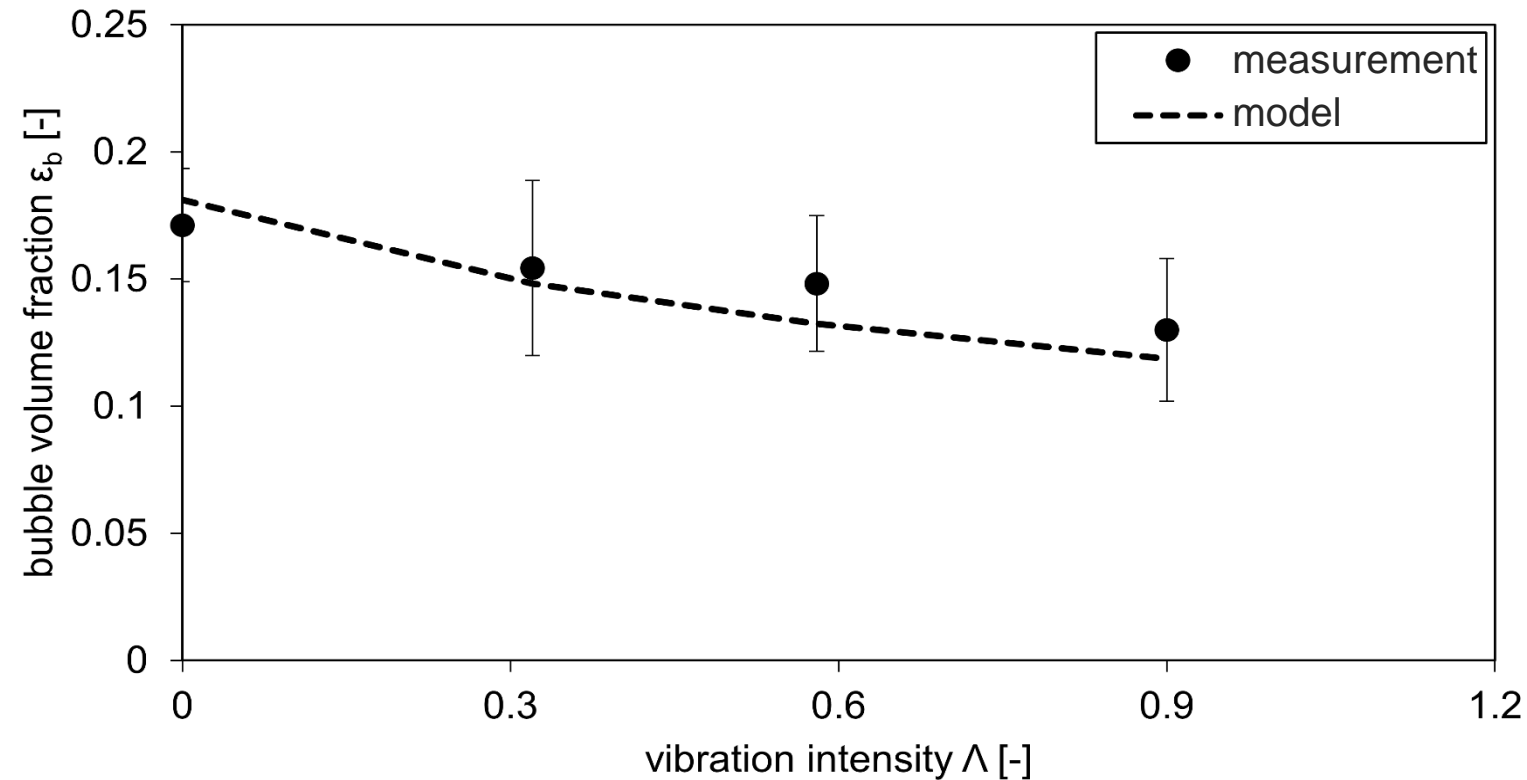
$$d_v = 0.21 \cdot \frac{(u - u_{mf})^{0.49} \cdot (h + 4\sqrt{A_0})^{0.48}}{g^{0.2}}$$

[8] Hillgardt and Werther, Ger. Chem. Eng. 9 (1986), 215-221

[9] Zou et al., Powder Technology 212 (2011), 258-266

Whole milk powder:

$x = 4 \text{ wt.-%}$ ,  $m = 25 \text{ kg}$ ,  $u = 0.2 \text{ m/s}$



red: adjustments to established correlations

**bold:** vibration dependent parameter

$d_v$ : bubble diameter;  $h$ : height over distributor;  $\varepsilon_b$ : local bubble volume fraction;  $u_b$ : bubble rise velocity;  $g$ : gravitational acceleration;  $\vartheta$ : hydrodynamic constant;  $u$ : gas velocity;  $u_{mf}$ : minimum fluidization velocity;  $\dot{V}_b$ : apparent gas flow rate per bubble cross sectional area;  $\Psi$ : hydrodynamic parameter for bed dimensions;  $A_0$ : cross sectional area of distributor orifices ( $A_0 \approx 0$  for porous plate)

Whole milk powder:  $x = 4$  wt.-%,  $m = 25$  kg

## Bed porosity:

$$\varepsilon = 1 - (1 - \varepsilon_b)(1 - \varepsilon_d)$$

## Porosity of dense phase:

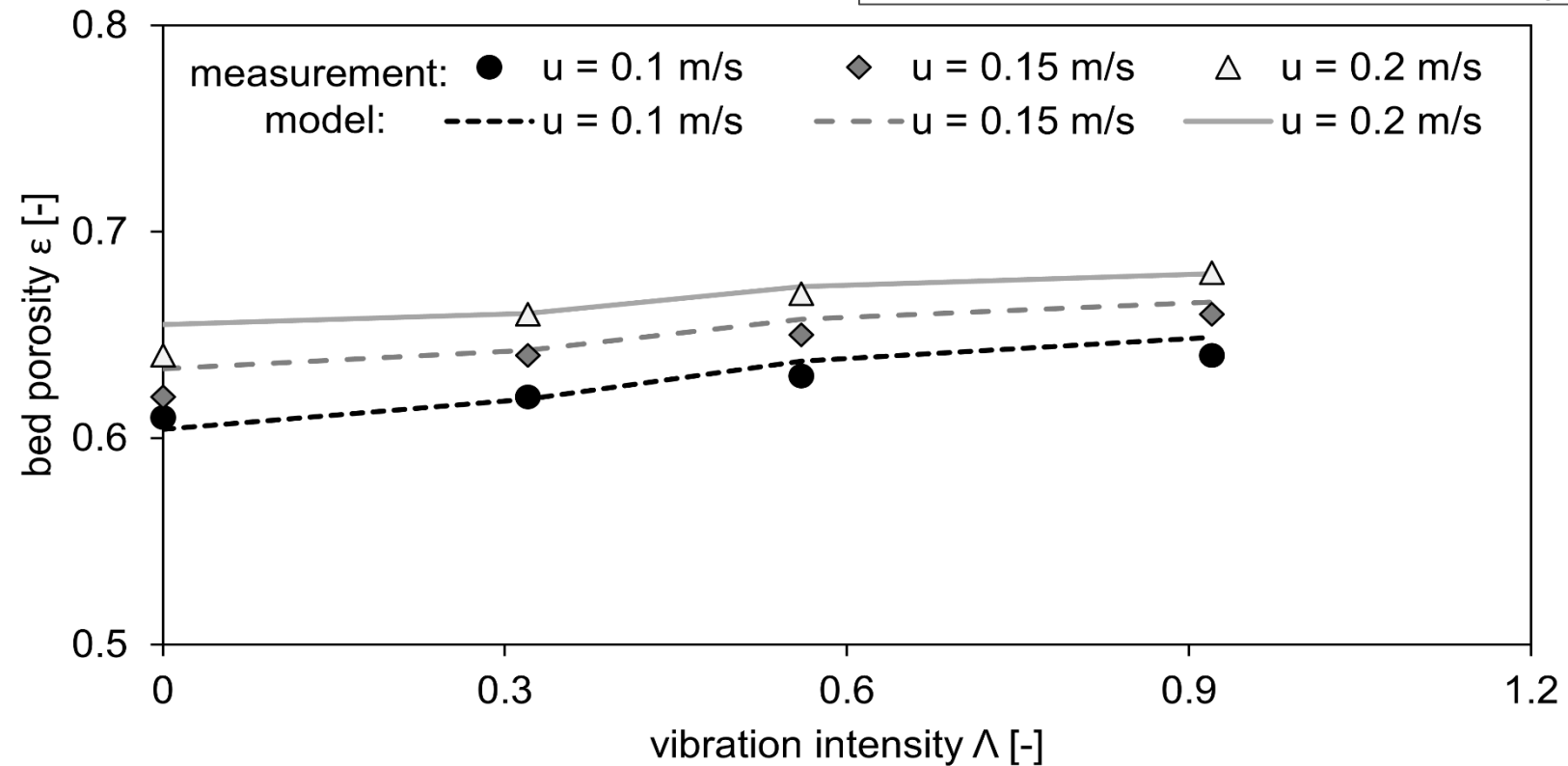
- modified Richardson and Zaki correlation [10]

$$\varepsilon_d = \varepsilon_{mf} \cdot \left( \frac{u_d}{u_{mf}} \right)^{\frac{1}{4.65 \cdot (1 + \Lambda)}}$$

## Gas velocity in dense phase:

- according to Clift et al. [11]

$$u_d = u_{mf} \cdot (1 + 1.5 \cdot \varepsilon_b)^{\frac{2}{3}}$$



red: adjustments to established correlations

**bold:** vibration dependent parameter

## Set of modified correlations:

- good prediction of  $\varepsilon_b$  and  $\varepsilon$  under vibration

[10] Richardson and Zaki, Chem. Eng. Sci., 3 (1954), 65-73

[11] Clift et al., Fluidization 4 - Proceedings, (1983), 77-85

$\varepsilon$ : bed porosity;  $\varepsilon_d$ : porosity of dense phase;  $\varepsilon_b$ : local bubble volume fraction;  $\varepsilon_{mf}$ : bed porosity at minimum fluidization;  $u_d$ : gas velocity in dense phase;  $\Lambda$ : vibration intensity;  $u_{mf}$ : minimum fluidization velocity



## Summary:

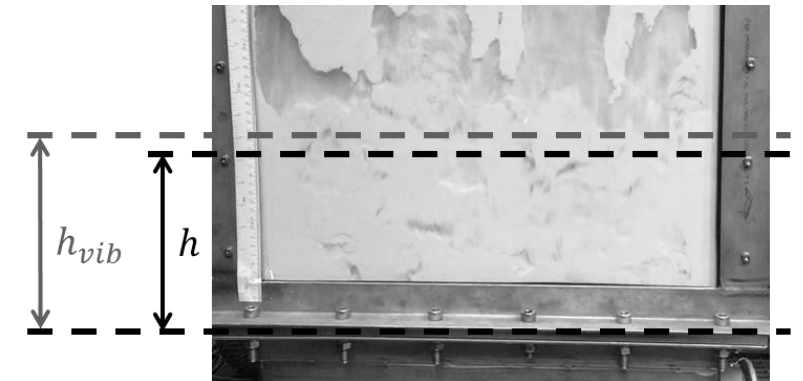
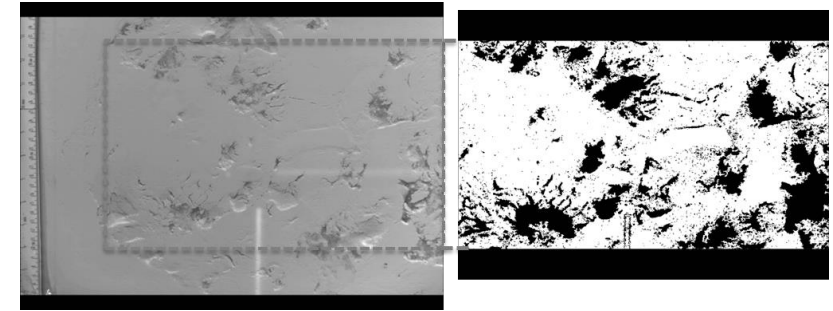
Pilot plant scale VFB dryer for comprehensive experiments:

Effect of vibration:

- reduces  $u_{mf}$
- reduces bubble volume fraction
- increases bed expansion
- expansion of suspension phase

Modeling of hydrodynamics under vibration:

- set of modified correlations for prediction of
  - bubble volume fraction
  - bed porosity
- correlation are unchanged for non-vibrated cases



## Outlook:

- testing model for other cohesive powders
- dynamic modeling of VFB dryers

Thank you  
for your attention!